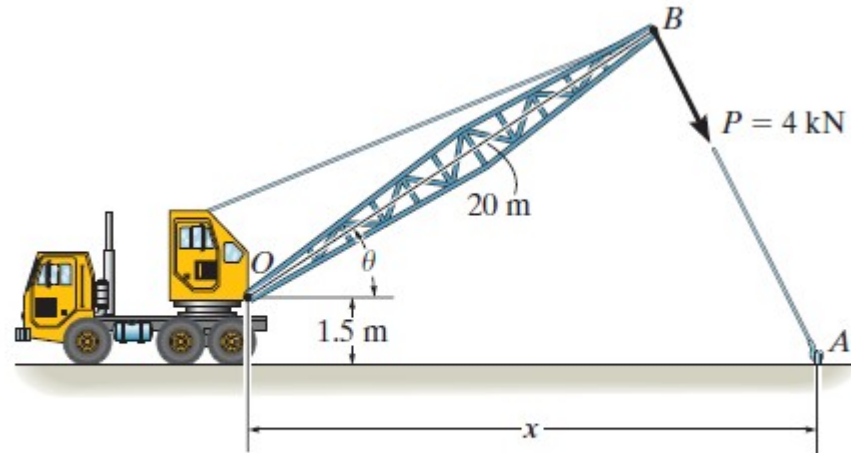


2º) Lista de exercício

A carga $P = 4\text{ kN}$ é aplicada na lança de 20 m se $x = 25$, determine ângulo θ para obter o maior valor de momento no ponto O .



Maximum moment, $OB \perp BA$

$$\sum + (M_O)_{max} = 4000(20) = 80\,000 \text{ N}\cdot\text{m} = 80.0 \text{ kN}\cdot\text{m} \quad \text{Ans}$$

$$4000 \sin \phi (25) - 4000 \cos \phi (1.5) = 80\,000$$

$$25 \sin \phi - 1.5 \cos \phi = 20$$

$$\phi = 56.43^\circ$$

$$\theta = 90^\circ - 56.43^\circ = 33.6^\circ \quad \text{Ans}$$

Also,

$$(1.5)^2 + z^2 = y^2$$

$$2.25 + z^2 = y^2$$

Similar triangles

$$\frac{20+y}{z} = \frac{25+z}{y}$$

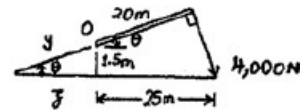
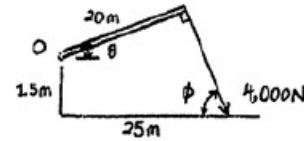
$$20y + y^2 = 25z + z^2$$

$$20(\sqrt{2.25 + z^2}) + 2.25 + z^2 = 25z + z^2$$

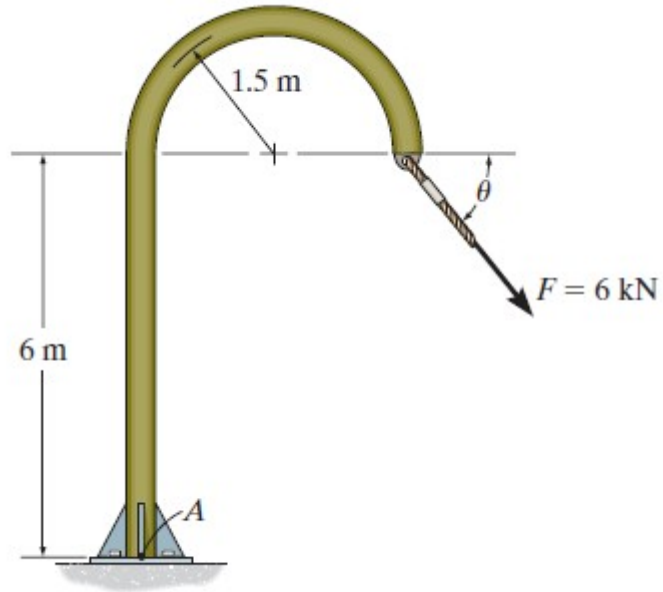
$$z = 2.259 \text{ m}$$

$$y = 2.712 \text{ m}$$

$$\theta = \cos^{-1}\left(\frac{2.259}{2.712}\right) = 33.6^\circ \quad \text{Ans}$$



Determine o momento produzido pela F no ponto A em termos do ângulo



Moment Function: Resolving force F into horizontal and vertical components, Fig. a , and applying the principle of moments,

$$\begin{aligned} \left(+M_A \right. &= -6 \cos \theta (6) - 6 \sin \theta (3) \\ &= -(36 \cos \theta + 18 \sin \theta) \text{ kN} \cdot \text{m} \\ &= (36 \cos \theta + 18 \sin \theta) \text{ kN} \cdot \text{m} \text{ (clockwise)} \end{aligned}$$

The maximum moment occurs when $\frac{dM_A}{d\theta} = 0$.

$$\frac{dM_A}{d\theta} = -36 \sin \theta + 18 \cos \theta = 0$$

$$\theta = 26.6^\circ$$

The maximum moment of F about point A is given by

$$(M_A)_{\max} = 36 \cos 26.57^\circ + 18 \sin 26.57^\circ = 40.2 \text{ kN} \cdot \text{m}$$

Also,

$$M_A \Big|_{\theta=0^\circ} = 36 \cos 0^\circ + 18 \sin 0^\circ = 36 \text{ kN} \cdot \text{m}$$

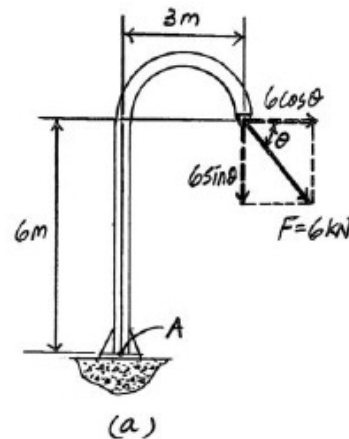
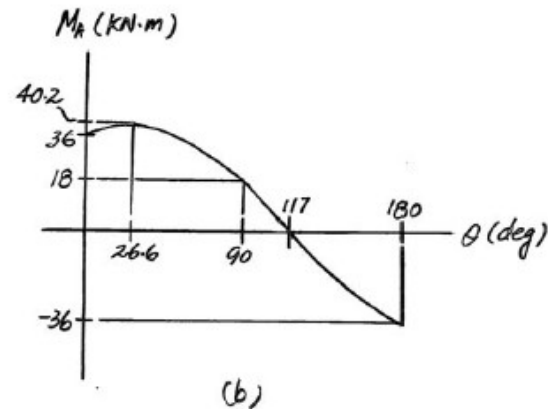
$$M_A \Big|_{\theta=90^\circ} = 36 \cos 90^\circ + 18 \sin 90^\circ = 18 \text{ kN} \cdot \text{m}$$

$$M_A \Big|_{\theta=180^\circ} = 36 \cos 180^\circ + 18 \sin 180^\circ = -36 \text{ kN} \cdot \text{m}$$

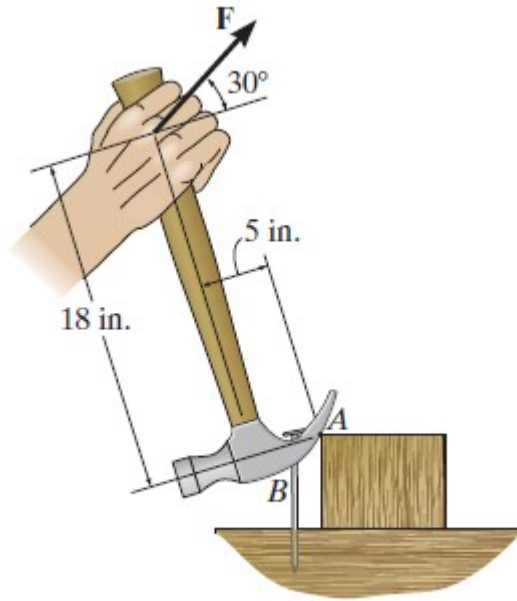
When $M_A = 0$,

$$0 = 36 \cos \theta + 18 \sin \theta \qquad \theta = 117^\circ$$

The plot of M_A versus θ is shown in Fig. b .



O martelo esta sujeito a força de 20 N, determine o momento no ponto A

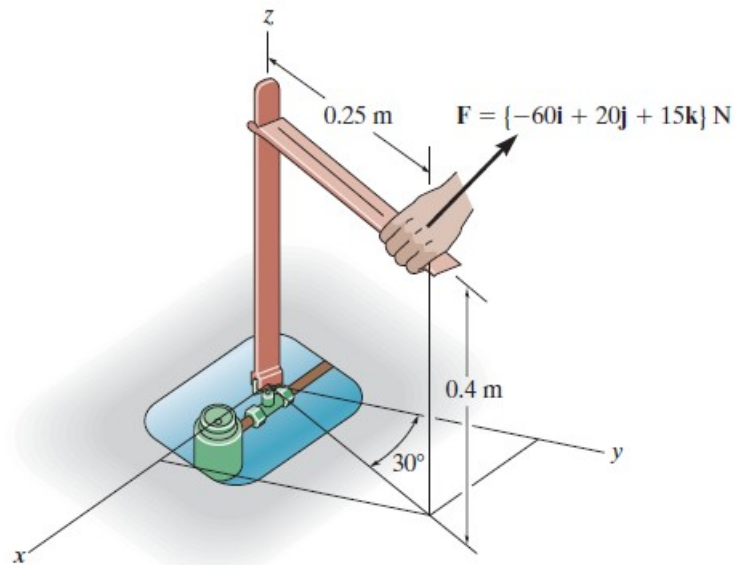


Resolving the 20 - lb force into components parallel and perpendicular to the hammer, Fig. *a*, and applying the principle of moments,

$$\begin{aligned} \sum +M_A &= -20 \cos 30^\circ(18) - 20 \sin 30^\circ(5) \\ &= -361.77 \text{ lb}\cdot\text{in} = 362 \text{ lb}\cdot\text{in} \text{ (clockwise)} \end{aligned}$$

Ans.

A ferramenta é usada na válvula de gas, por causa do difícil acesso, determine Os momentos gerados



$$\mathbf{u} = \mathbf{k}$$

$$\mathbf{r} = 0.25 \sin 30^\circ \mathbf{i} + 0.25 \cos 30^\circ \mathbf{j}$$

$$= 0.125 \mathbf{i} + 0.2165 \mathbf{j}$$

$$M_c = \begin{vmatrix} 0 & 0 & 1 \\ 0.125 & 0.2165 & 0 \\ -60 & 20 & 15 \end{vmatrix} = 15.5 \text{ N}\cdot\text{m} \quad \text{Ans}$$